

Modern Methods in Heterogeneous Catalysis Research

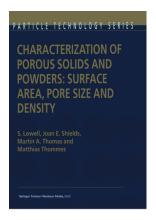


Surface area and pore size determination

24 November 2017 Annette Trunschke

Further reading

S. Lowell, J.E. Shields, M.A. Thomas, M. Thommes, Characterization of Porous Solids and Powders: Surface Area, Pore Size and Density, Kluwer Academic Publisher, Dordrecht, 2004, Springer 2006.

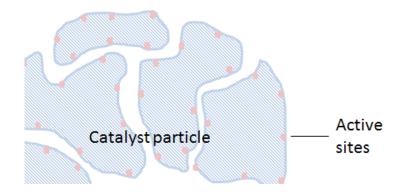


- R. Brdička, Grundlagen der physikalischen Chemie, Deutscher Verlag der Wissenschaften, Berlin 1982. P.W. Atkins, J. de Paula, Physikalische Chemie, Wiley-VCH, Weinheim 2013.
- G. Wedler, H.-J. Freund, Lehrbuch der Pysikalischen Chemie, Wiley-VCH, 2012.
- F. Schüth, K.S.W. Sing, J. Weitkamp (Eds.), Handbook of Porous Solids, Vol. 1, Wiley-VCH, Weinheim 2002.
- G. Ertl, H. Knözinger, J. Weitkamp (Eds.), Handbook of Heterogeneous Catalysis, VCH, Weinheim, 1997.



Heterogeneous catalysis

- Heterogeneous catalysis happens at the interface between phases
- The number of active sites depends on the surface area
- Surface area is related to
 - Particle size
 - Particle morphology
 - Surface texturing
 - Porosity



- The accessibility of active sites requires pores that allow molecular transport
- Porosity: fraction of the total void volume with respect to the

volume of the catalyst

- Texture: pore size
 - pore size distribution
 - pore shape

Heterogeneous catalysis

600-800°C

 $(NH_4)_2[PtCl_6]$

 \longrightarrow

Pt with high surface area



$$2 H_2 + O_2 \rightarrow$$

 $2 H_2O$



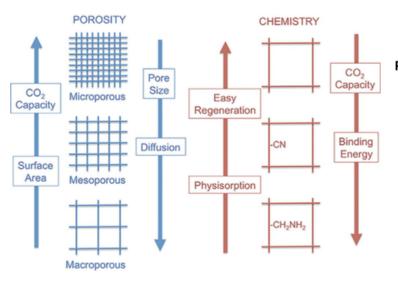
Johann Wolfgang Döbereiner 's lighter (1823)

Some catalysts and support materials in heterogeneous catalysis

adsorbent	surface area [m²/g]
charcoal	300 - 2500
silica gel	300 -350
γ-alumina	200 - 500
zeolites	500 - 1100

High surface area materials

Table 2. List of leading CO ₂ capture sorbents.						
Supporting porous material	Amine type	[mm	sorption ol g^{-1}] Wet CO_2	(adsorption-desorption)	Sorption partial pressure of CO ₂ [bar] (adsorption–desorption)	
MCM-41 ^[11]	Polyethylenimine	2.02	2.98	75–75	0.15–0	
SBA-15 ^[12]	(3-Trimethoxysilylpropyl) diethylenetriamine	2.4	2.72	60->300	0.15–0	
Mesoporous silica capsules[13]	Tetraethylenepentamine	-	7.93	75-100	0.1–0	
Mesoporous silica foam ^[14]	Tethered amines	-	11.8	25–100	0.08–0	
Mg-MOF-74 ^[15]	N,N'-Dimethyl ethylene diamine (mmen)	3.1	2.7	40-120	0.15–0	
PPN-6- CH₂DETA ^[16]	Linear amines	3.04	-	22–80	0.15–vacuum	
COP-19 ^[17]	Polyethylenimine	1.57	2.27	40-80	0.15–vacuum	
Hollow fibres (continuous)[18]	Amine impregnated silica	-	0.58	35-120	0.1–0	
Aqueous amines[19]	Monoethanolamine (MEA)	-	0.83	80/120-120	0.15–0	



Dry condition (carbamate formation)

Primary amines

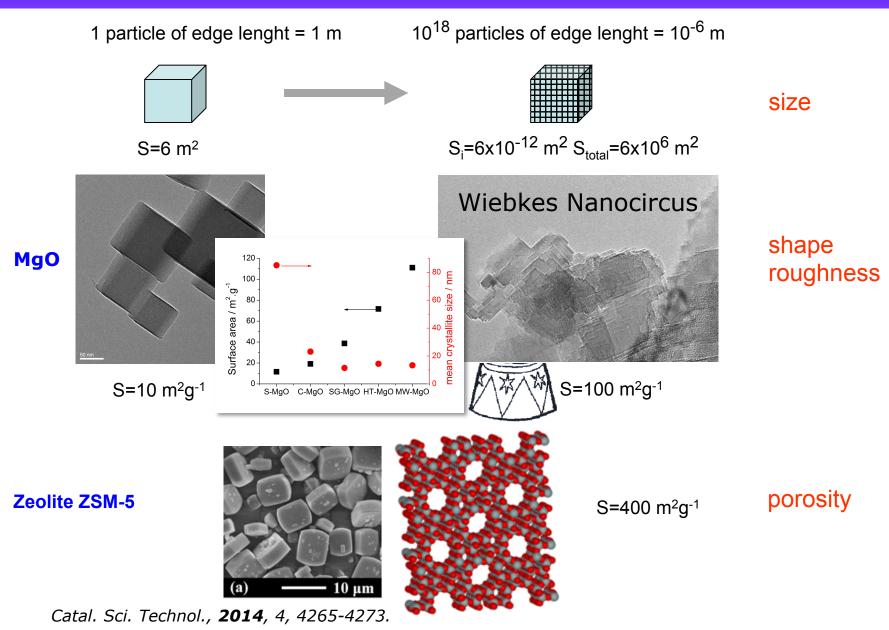
Humid condition (bicarbonate formation)

Table 3. Benchmark checkpoints for an effective ${\rm CO_2}$ sorbent. All conditions have to be met to get the best working sorbent.

Checkpoint	Desired
Capacity	>2 mmol CO ₂ per g of sorbent
Recyclability	>1000 cycles
Selectivity	> 100 (CO ₂ /other gases)
Stability	> 150 °C, boiling water, H ₂ S, SO _x , NO _x , HCl, NaOH,
	mechanical strength with low attrition index (AI)
Cost	< \$50 kg ⁻¹ (sorbent cost $<$ \$10 kg ⁻¹)
Kinetics	>1 mmol(g×min) ⁻¹

ChemSusChem 2017, 10, 1303 - 1317.

Factors affecting surface area



Surface area measurements

Surface area from particle size distribution

Dynamic light scattering

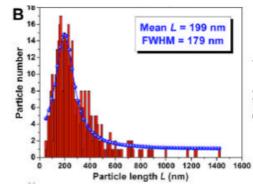
Measures Brownian motion and relates this to the size of the particles by using a correlation function and the Stokes-Einstein equation

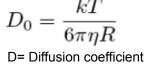
Non-spherical particles will be measured as equivalent spheres

Microscopy

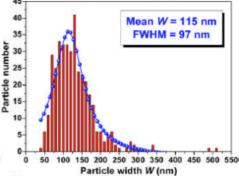
Shape analysis







k= Boltzmann constant
T= absolute temperature
η= dynamic viscosity of the solvent
R= radius of the particle

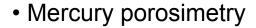


Small angle X-ray scattering

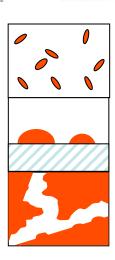
Scattering of X-rays by small domains of uniform matter (crystalline or amorphous), for which the electron density ρ^{e} is different from the continuous medium

The central peak of scattered intensity gets broader as the domain size (particles, voids) decreases

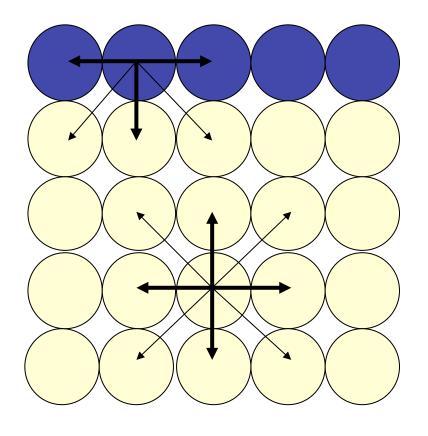
SAXS parameters (mean size / size distribution / specific surface area) are derived from analysis of the profile of the SAXS curve



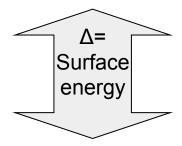
Intrusion of a non-wetting liquid (often Hg) at high pressure, measurement based on the external pressure needed to force the liquid into a pore against the opposing force of the liquid's surface tension, Inner surface of porous materials, pore width > 2nm



Adsorption - driving forces



Surface atom – unbalanced forces



Bulk atom – balanced forces

Adsorption: a substance is enriched at the interface between two phases with respect to its concentration in the homogeneous phase

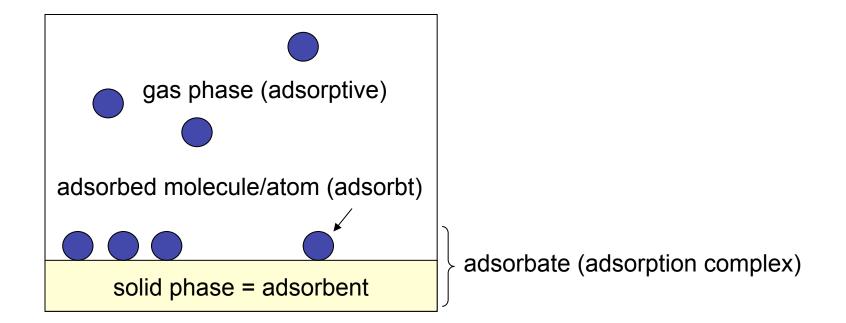
Involved forces

- Formation of a chemical bond (chemisorption)
- Van der Waal's forces (physisorption)
- 1. Dispersion forces* (major part of the interaction potential)

 The electron motion in an atom or molecule leads to a rapidly oscillating dipole moment coupling of two neighboring moments into phase leads to a net attractive potential
- 2. Ion-dipole (ionic solid/polar gas molecule)
- 3. Ion-induced dipole (polar solid/polarizable gas molecule)
- Dipole-dipole (polar solid/polar gas molecule)
- Quadrupole interactions (symmetrical molecules, e.g., ⁻O-C++-O-)
- * F. London, Z. Phys. 63 (1930) 245.

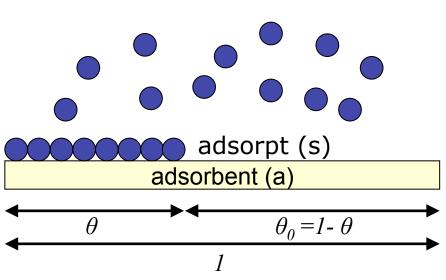
Similar to forces that lead to liquifidation of vapors

Adsorption



Description of adsorption

Relation between T, p, adsorbed amount (surface concentration)



$$\Gamma = n_{\rm s}/s_{\rm a}$$
 $\gamma = n_{\rm s}/m_{\rm a}$
 $\Gamma = \gamma/S_{\rm a,sp.}$
 $W_{\rm s}$
 $V_{\rm s}$

Fraction of occupied surface (coverage)

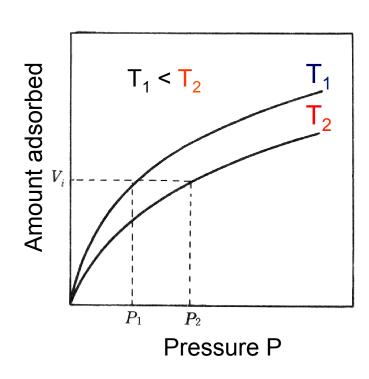
$$\theta = \Gamma / \Gamma_{\rm m} = \gamma / \gamma_{\rm m} = N / N_{\rm m} = W / W_{\rm m}$$

$$\Gamma = f(p) < eq.$$
, $T = const. > adsorption isotherm$
 $\Gamma = f(T) < eq.$, $p = const. > adsorption isobar$
 $p = f(T) < eq.$, $\Gamma = const. > adsorption isostere$

Adsorption isotherm

$$\Gamma = f(p)_T$$

Adsorption is favored at lower temperatures



$$\Delta G = \Delta H - T \Delta S$$

Decrease in translation freedom by adsorption: $\Delta S<0$ Adsorption is a spontaneous process: $\Delta G<0$

ΔH<0 Exothermic process

Volumetric measurement

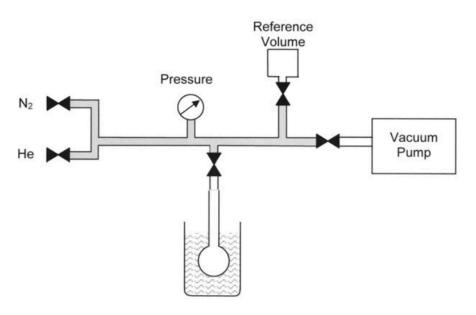


Figure 14.1b Simplified, modern static volumetric apparatus.

- Application of ideal gas equation
- Void volume determination by He:
- (i) He does not adsorb
- (ii) He does not penetrate into regions which are inaccessible for the adsorptive
- The pressure is expressed as a fraction of the saturation pressure p_0 that is defined as the saturated equilibrium vapor pressure exhibited by the pure adsorptive contained in the sample at the adsorption temperature
- The saturation pressure depends on the temperature Clausius-Clapeyron:

 $\ln(p_{0.T2}/p_{0.T1}) = \Delta H/R(1/T_1-1/T_2)$

$$V_s$$
 volume sorbed V_d volume of adsorptive dosed V_m volume of manifold V_v volume of the sample cell, which is not occupied by the adsorbent p_m manifold pressure before the dose p_{eq} equilibrium pressure after the dose T_{eq} temperature in equilibrium

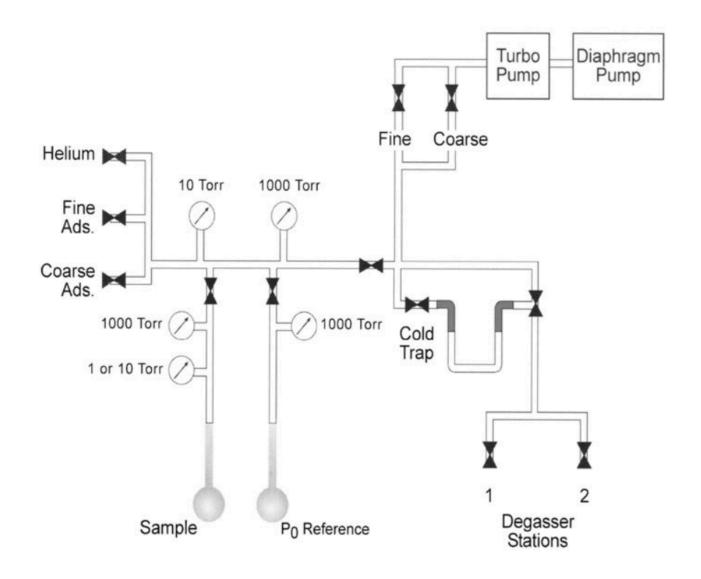
$$V_{d} = \left(\frac{p_{m}V_{m}}{T_{m}} - \frac{p_{eq}V_{m}}{T_{eq}}\right) \times \left(\frac{T_{Std}}{p_{Std}}\right)$$

$$V_s = V_d - \left(\frac{p_{eq} V_{v77K}}{p_{Std}}\right)$$

$$T_{std} = 273.15 \text{ K}, p_{std} = 760 \text{ torr}$$

$$V_{stp}[\text{cm}^3]/22414 \text{ cm}^3 = n_s$$

Volumetric measurement

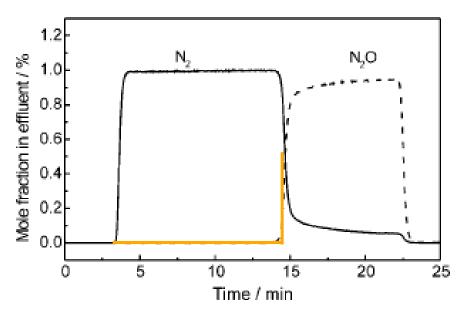


Dynamic methods

Continuous flow technique (frontal sorption method)

$$N_2O(g) + 2Cu_s^0 \rightarrow (Cu - O - Cu)_s + N_2(g)$$

 $\Delta_R H = 317 \text{ kJ/mol}$ (N₂O, Cu/ZnO)



Cu/ZnO/Al₂O₃ catalyst

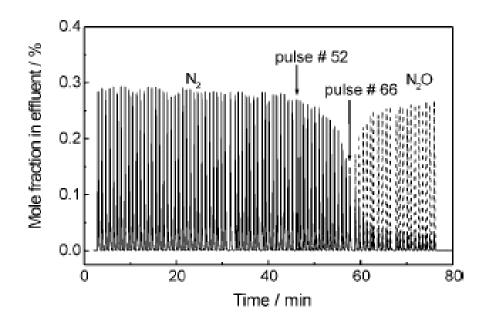
- Flow of 10 Nml/min 1% N₂O/He at 300 K, p=0.1 MPa, m_{cat}=0.2 g bed height=20 mm contact time = 1.4 s ΔT approx. 1 K
- Determination of N₂ formed as product of molar flow and peak area by TCD/MS

O. Hinrichsen, T. Genger, and M. Muhler, Chem. Eng. Technol. 23 (2000) 11.

Dynamic methods

Pulse technique (pulse sorption method)

$$N_2O(g) + 2Cu_s^0 \rightarrow (Cu - O - Cu)_s + N_2(g)$$



Cu/ZnO/Al₂O₃ catalyst

Injection of successive small pulses of known volume into the flow of an inert gas

- Flow of 20 Nml/min He $V = 1.0 \text{ ml N}_2\text{O}$ T = 300 K p=0.1 MPa
- #66= 125 µmol/g N₂

O. Hinrichsen, T. Genger, and M. Muhler, Chem. Eng. Technol. 23 (2000) 11.

Gravimetric techniques

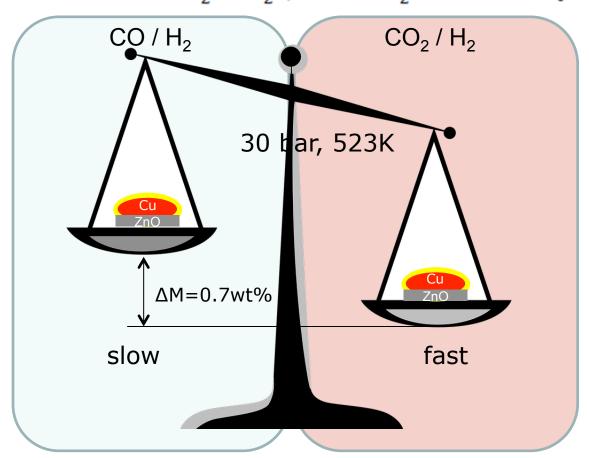
$$CO_2 + 3H_2 \not\subset CH_3OH + H_2O \quad \Delta H_0 = -49.8 \, kJ/mol \, (1)$$

$$CO + 2H_2 \rightleftarrows CH_3OH$$

$$\Delta H_0 = -91.0 \, kJ/mol \, (2)$$

$$CO_2 + H_2 \neq CO + H_2O$$

$$\Delta H_0 = +41.2 \, kJ/mol \, (3)$$



Andrey Tarasov

Gravimetric techniques

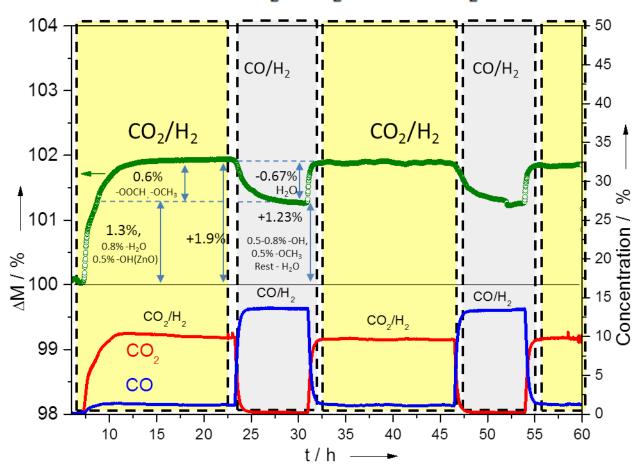
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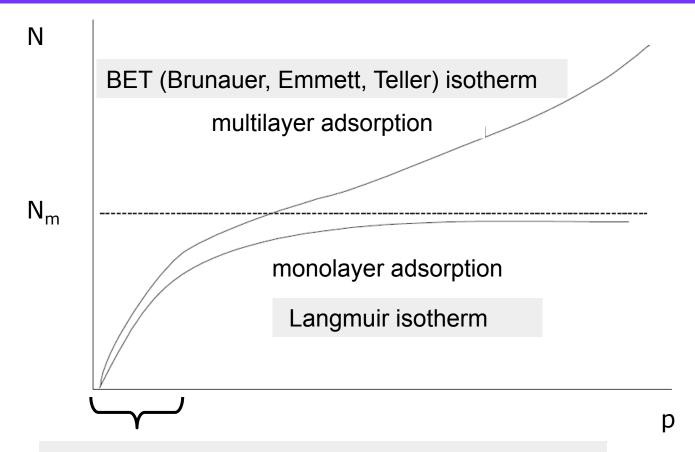
$$CO_2 + H_2 \neq CO + H_2O$$

$$\Delta H_0 = +41.2 \, kJ/mol \, (3)$$



Andrey Tarasov

Adsorption isotherms



 Freundlich isotherm (interaction of adsorbed molecules)

$$\theta = c_1 p^{1/c2}$$

• Temkin isotherm (adsorption enthalpy is a function of the pressure) $\theta = c_1 ln(c_2 p)$

Adsorption isotherm

- Mathematical description of the adsorption isotherms allows to determine
 - Monolayer capacity
 - Surface area
 - Pore data
- The models used for mathematical description are often empirical models that fit more or less to experimental data
- The results are useful and required to interpret catalytic data
- Please consider in the discussion of your results that the surface area or the pore volume determined by using the various empirical models are approximated values

Surface area measurements

$$S = A_x N_m$$

 A_x cross-sectional area of the adsorbed molecule

• Nitrogen 0.162 nm²

• Argon 0.166 nm²

• Krypton 0.210 nm²

 $N_{\it m}$ number of adsorbate molecules required to cover the solid with a single monolayer

Theories that give access to the monolayer capacity using the isotherm

- Langmuir
- BET

Langmuir isotherm*

Assumptions

- Monolayer adsorption
- Energetically uniform surface
- No interactions between adsorbed species - heat of adsorption independent of coverage

[CONTRIBUTION FROM THE RESEARCH LABORATORY OF THE GENERAL ELECTRIC CO.]

THE ADSORPTION OF GASES ON PLANE SURFACES OF GLASS, MICA AND PLATINUM.

BY IRVING LANGMUIR. Received June 25, 1918.

In his studies of the continuous change from the liquid to the vapor state, at temperatures above the critical, van der Waals developed the theory that at the boundary between a liquid and its vapor there is not an abrupt change from one state to the other, but rather that a transition layer exists in which the density and other properties vary gradually from those of the liquid to those of the vapor.

This idea of the continuous transition between phases of matter has been applied very generally in the development of theories of surface phenomena, such as surface tension, adsorption, etc.

Eucken, for example, in dealing with the theory of adsorption of gases, considers that the transition layer is a sort of miniature atmosphere, the molecules being attracted to the surface by some kind of "action at a

¹ Eucken, Verh. deut. physik. Ges., 16, 345 (1914).

Kinetic expression of the adsorption equilibrium

$$\mathbf{r}_{ads} = \mathbf{r}_{des}$$

$$dN_{ads} = dN_{des}$$

I. Langmuir, J. Am. Chem. Soc. 40 (1918) 1361.

Langmuir isotherm

$$A + * \frac{k_A^+}{\langle k_A^- \rangle} A^*$$

$$\frac{d\theta_A}{dt} = p_A k_A^+ (1 - \theta_A) - k_A^- \theta_A$$

$$K_A = \frac{k_A^+}{k_A^-}$$

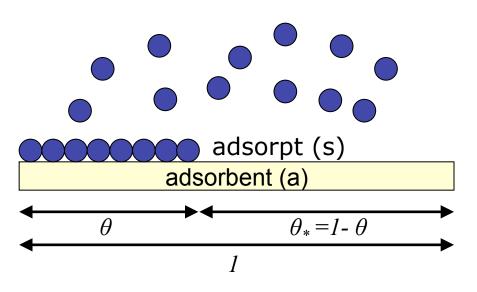
in equilibrium:

$$p_A k_A^+ (1 - \theta_A) = k_A^- \theta_A$$

$$\theta_A = \frac{K_A p_A}{1 + K_A p_A}$$

$$\theta_* = (1 - \theta_A) = \frac{1}{1 + K_A p_A} \implies \theta_A = K_A p_A \theta_*$$



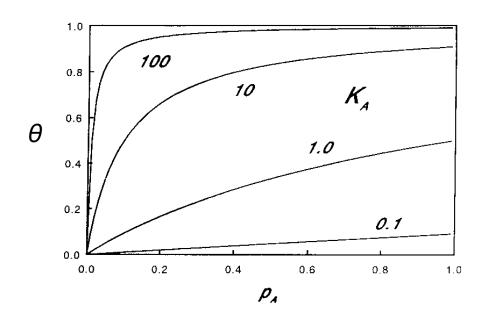


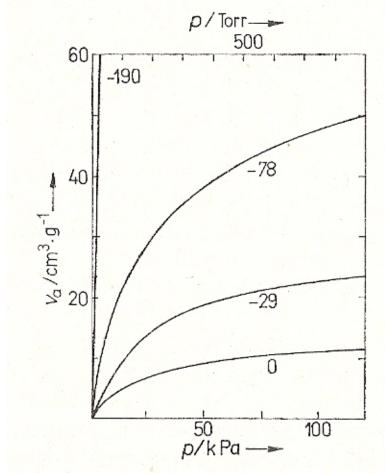
Irving Langmuir Nobel Prize in Chemistry in 1932

Langmuir isotherm

$$\theta = \frac{N}{N_m} = \frac{K p}{1 + K p}$$

$$K = \frac{k_{ads}}{k_{des}}$$





Adsorption of nitrogen on charcoal at different T

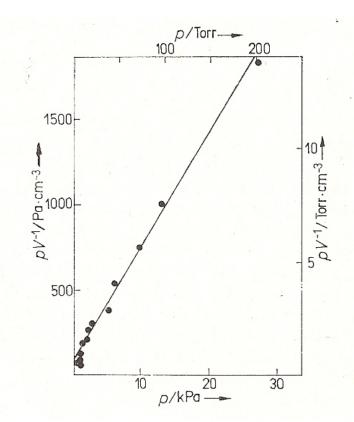
$$\left(\frac{\partial \ln K}{\partial T}\right)_{\Theta} = \frac{\Delta_{ads}H}{RT^2}$$

Langmuir isotherm

$$\theta = \frac{N}{N_m} = \frac{K p}{1 + K p}$$

Linear plot

$$\frac{p}{N} = \frac{1}{KN_m} + \frac{p}{N_m}$$



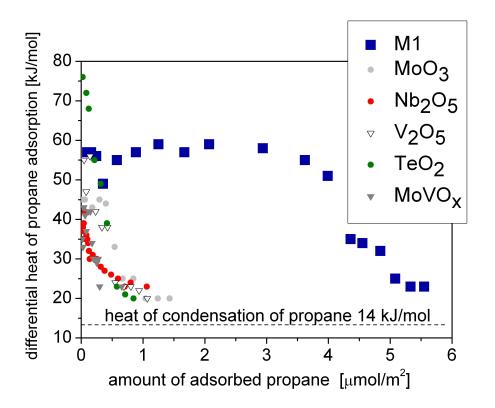
$$n = \frac{N}{N_A} = \frac{m_m}{M_{asdorptive}}$$

$$S = N_m A_x = \frac{m_m N_A A_x}{M_{asdorptive}}$$

Abb. 6.47 Linearisierte Langmuirsche Adsorptionsisotherme für die Adsorption von Wasserstoff an Kupferpulver bei $25\,^{\circ}$ C

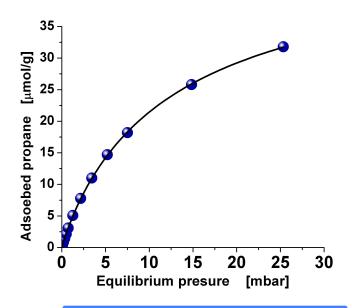
Langmuir isotherm - adsorption of propane on oxides

M. Hävecker et al., Journal of Catalysis 285 (2012) 48-60.



Cross-sectional area of propane: 36 Å²

Adsoption isotherm of propane over M1 at T=313 K



$$K = 0.111(6) \text{ hPa}^{-1}$$
 $N_m = 43 \text{ } \mu \text{mol } \text{g}^{-1}$
 $S_{\text{Langmuir}} = 9.2 \text{ } \text{m}^2 \text{ } \text{g}^{-1}$
 $S_{\text{BET}} = 8.8 \text{ } \text{m}^2 \text{ } \text{g}^{-1}$

- A.L. McClellan, H.F. Harnsberger, J. Colloid Interface Sci. 23 (1967) 577.
- S.J. Gregg, R. Stock, Trans. Faraday Soc. 53 (1957) 1355.

Other isotherms - C3H8 adsorption on CNTs - Temkin

B. Frank et al., ChemPhysChem 12 (2011) 2709 - 2713.

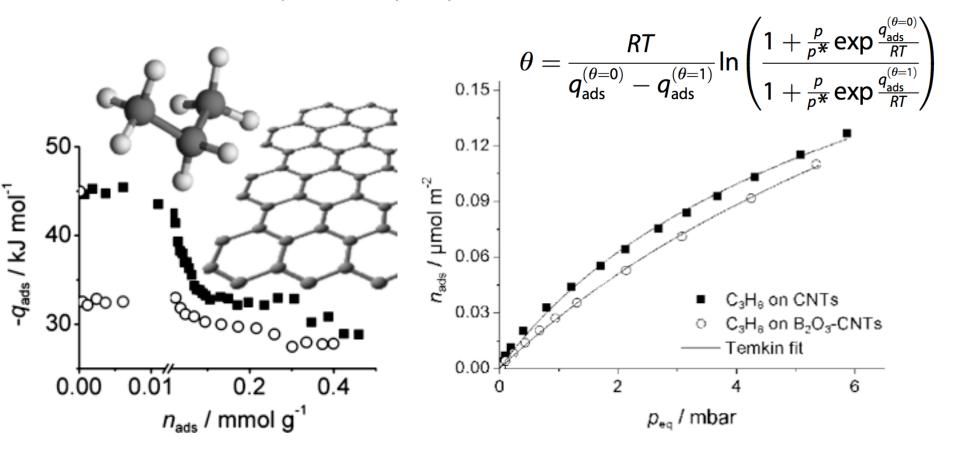


Figure 3. Isotherms of propane adsorption (313 K) on the oxygen surface groups of CNT and B_2O_3 –CNT catalysts used in ODH of propane.

M. I. Temkin, Zhur. Fiz. Khim. 15 (1941) 296.

Adsorption isotherms

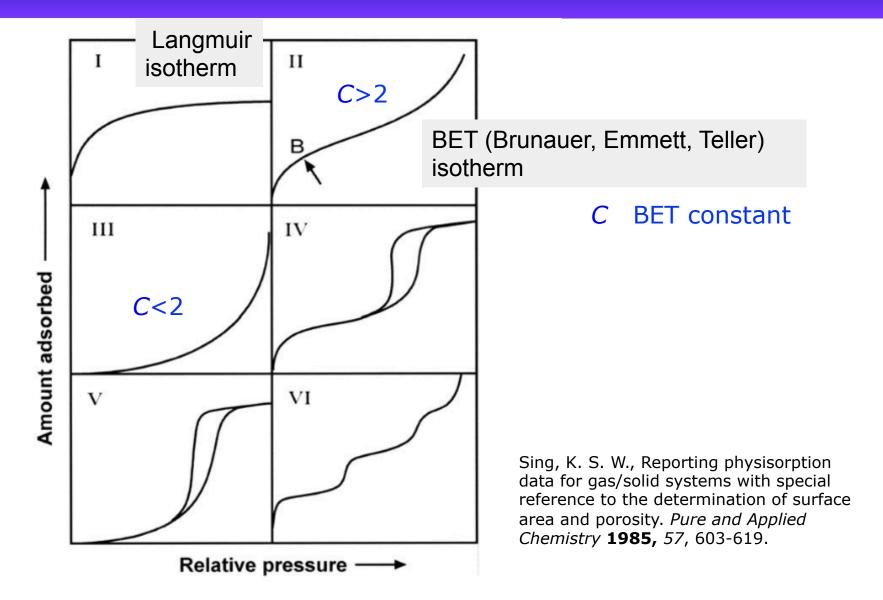


Figure 3.2 IUPAC classification of sorption isotherms. From [1].

Feb., 1938

Adsorption of Gases in Multimolecular Layers

309

[CONTRIBUTION FROM THE BUREAU OF CHEMISTRY AND SOILS AND GEORGE WASHINGTON UNIVERSITY]

Adsorption of Gases in Multimolecular Layers

By Stephen Brunauer, P. H. Emmett and Edward Teller

Introduction

The adsorption isotherms of gases at temperatures not far removed from their condensation points show two regions for most adsorbents: at low pressures the isotherms are concave, at higher pressures convex toward the pressure axis. The higher pressure convex portion has been variously interpreted. By some it has been attributed to condensation in the capillaries of the adsorbent on the assumption that in capillaries of molecular dimensions condensation can occur at pressures far below the vapor pressure of the liquid. By others such isotherms are believed to indicate the formation of multimolecular adsorbed layers. DeBoer and Zwicker1 explained the adsorption of non-polar molecules on ionic adsorbents by assuming that the uppermost layer of the adsorbent induces dipoles in the first layer

I. The Polarization Theory of DeBoer and Zwicker

According to DeBoer and Zwicker, the induced dipole in the *i*th layer polarizes the i + 1st layer, thus giving rise to induced dipole moments and binding energies that decrease exponentially with the number of layers. If we call the dipole moment of a molecule in the *i*-th layer μ_i , it follows that

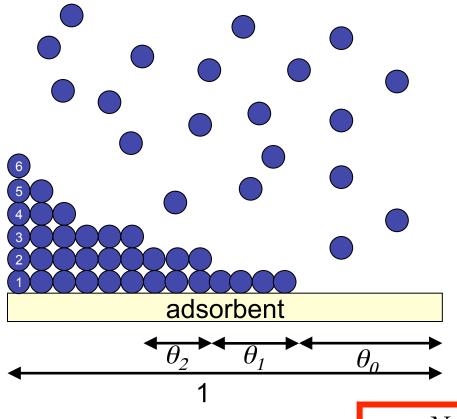
$$\mu_i = c_1 C^i \tag{1}$$

where c_1 and C are appropriate constants, C actually being equal³ to μ_i/μ_{i-1} . The corresponding binding energy is proportional to the square of the dipole moment

$$\phi_i = c_2 C^{2i} \tag{2}$$

where c_2 is another constant. The equilibrium pressure of the *n*th layer (top layer), p_n , according to Boltzmann's law varies exponentially with the

* S. Brunauer, P.H. Emmett, E. Teller, J. Am. Chem. Soc. 60 (1938) 309.



Description of all isotherm types

Assumptions

- Multilayer adsorption
- First layer: Langmuir adsorption
- Second and further layers: condensation of gas onto liquid
- Heat of adsorption:

First layer > second layer = ... = ... = heat of condensation

$$\theta = \frac{N}{N_m} = \frac{C \cdot (p/p_0)}{(1 - p/p_0) \cdot [1 - p/p_0 + C(p/p_0)]}$$

 p_0 ...vapor pressure of liquid N_2

* S. Brunauer, P.H. Emmett, E. Teller, J. Am. Chem. Soc. 60 (1938) 309.

$$\frac{1}{W[p/p_0-1]} = \frac{1}{W_m C} + \frac{C-1}{W_m C} \left(\frac{p}{p_0}\right)$$

W ... mass of adsorbed N₂

$$W_m = \frac{1}{S+i}$$

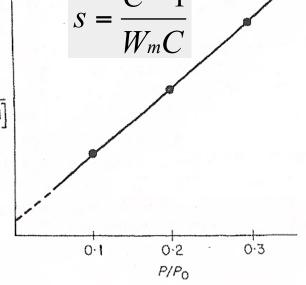
$$C = \frac{s}{i} + 1$$

$$S = \frac{W_m N_A A_x}{M_{adsorptive}}$$

$$S_{sp.} = \frac{S}{m}$$

$$i = \frac{1}{W_m C}$$

Relative pressures near completed monolayers $0.05 < p/p_0 < 0.3$



Single point BET

Assumption: For high values of C the intercept may be taken as zero

$$W_m = W\left(1 - \frac{p}{p_0}\right)$$

$$S = W \left(1 - \frac{p}{p_0} \right) \frac{N_A}{M_{adsorptive}} A_x$$

"Monolayer" coverage

$$\theta_0 = \frac{\sqrt{C} - 1}{C - 1} = \left(\frac{p}{p_0}\right)_m$$

$$C = 100$$

$$\theta_0 = \frac{\sqrt{100} - 1}{100 - 1} = 0.091$$

- The adsorbate is not necessarily arranged in neat stacks of various hight
- The numerical value of the relative pressure at which $W=W_m$ corresponds to the fraction of surface unoccupied by the adsorbate

The BET constant

$$\frac{W}{W_m} = \left(1 - \frac{p}{p_0}\right) + \frac{1}{C} \left(\frac{p}{p_0} + \frac{p_0}{p} - 2\right)$$

Table 5.3 Values of W/W_m and relative pressures for various values of C.

P/P_0	C = 0.05	C = 0.5	C = 1	C = 2	C = 3	C = 10	C = 100	C = 1000
0.02	0.001	0.010	0.020	0.040	0.059	0.173	0.685	0.973
0.05	0.003	0.027	0.052	0.100	0.143	0.362	0.884	1.030
0.10	0.006	0.058	0.111	0.202	0.278	0.585	1.020	1.100
0.20	0.015	0.139	0.250	0.417	0.536	0.893	1.200	1.250
0.30	0.030	0.253	0.429	0.660	0.804	1.160	1.400	1.430
0.40	0.054	0.417	0.667	0.952	1.110	1.450	1.640	1.660
0.50	0.095	0.667	1.000	1.330	1.500	1.820	1.980	2.000
0.60	0.172	1.060	1.490	1.870	2.040	2.340	2.480	2.500
0.70	0.345	1.790	2.330	2.740	2.910	3.190	3.320	3.330
0.80	0.833	3.330	4.000	4.440	4.620	4.880	4.990	5.000
0.90	3.330	8.330	9.090	9.520	9.680	9.900	9.990	10.000
0.94	7.350	14.700	15.700	16.200	16.300	16.600	16.700	16.700

Applicability of the BET theory

- In the region of relative pressures near completed monolayers (0.05<p/p₀<0.3) experiment and theory agree well → powerful method of surface area determination
- In the linear BET range the very high energy sites are occupied and extensive multilayer coverage has not yet commenced
- C<2: Better change the adsorbate

$$C = e^{(\Delta_{des}H - \Delta_{evac}H/RT)}$$

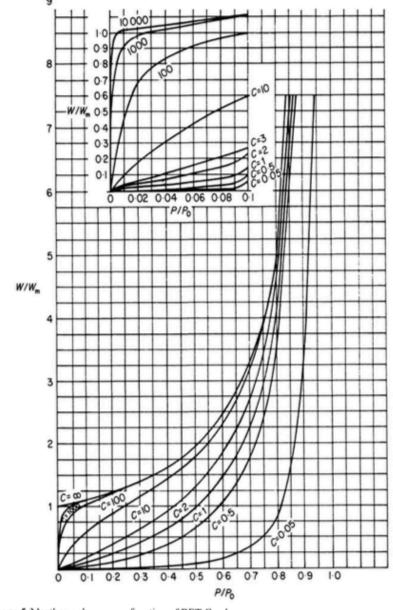
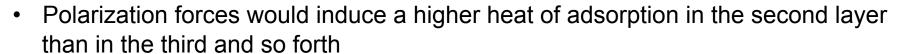


Figure 5.3 Isotherm shapes as a function of BET C values.

Applicability of the BET theory

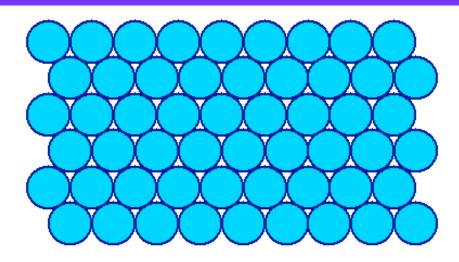
- BET theory ignores inhomogeneities of the surface and lateral adsorbate adsorbate interactions
 - High energy sites will be occupied at lower relative pressures
 - Reason for the nonlinearity of BET plots at $p/p_0 < 0.05$



- Reason for the failure of the BET equation at $p/p_0 > 0.3$
- The BET equation is applicable for surface area analysis of nonporous materials
 - Difficulties to separate mono-multilayer adsorption from pore filling
 - Filling of micropores is completed at $p/p_0 < 0.1$, however, linear BET plot are found at even lower relative pressures
 - \rightarrow measured surface area reflects not a real internal surface, but a ,, characteristic " BET surface area
 - For mesoporous materials exhibiting pore diameters between 2 and 4 nm (MCM-41, MCM-48) pore filling is observed at pressures close to mono-multilayer formation
 - → overestimation of monolayer capacity



Cross-sectional area



Closed-packed hexagonal arrangement of spheres

$$A_x = 1.091 \left(\frac{\overline{V}}{\overline{N}}\right)^{\frac{2}{3}} \times 10^6$$

 \overline{V} liquid molar volume

 \overline{N} Avogadro's number

 $(6.022 \times 10^{23} \text{ molecules per mole})$

Nitrogen as the standard adsorptive

- The cross sectional area depends on T, adsorbate-adsorbate, and adsorbentadsorbate interactions
- For most of the adsorbents the C constant for N₂ lies in the range from about 50 to 300 (no very weak interaction, no chemisorption)
- Its permanent quadrupole moment is responsible for the formation of welldefined monolayers on most of the surfaces
- Overestimation (20%!) of surface areas of hydroxylated silica surfaces due to specific interactions with the polar surface groups (use 13.5 Ų)

Langmuir, 1994, 10 (11), pp 4225-4231.

Cross-sectional area

Table 5.4 Cross-sectional areas of some frequently used adsorptives.

Adsorptive Temperature	Cross-sectional area (Å ²)[15]	Customary Value (Å ²)
Nitrogen 77.35 K	13.0 - 20.0	16.2
Argon 77.35 K	10.0 - 19.0	13.8 6.5 K below bulk triple point
Argon 87.27 K	9.7 - 18.5	14.2
Krypton 77.35 K	17.6 - 22.8	20.2
Xenon 77.35 K	6.5 - 29.9	16.8
Carbon Dioxide	14 - 22.0	
195 K		19.5
273 K		21.0
Oxygen 77.35 K	13 - 20	14.1
Water 298.15 K	6 - 19	12.5
n-Butane 273.15 K	36 - 54	44.4
Benzene 293.15 K	73 - 49	43.0

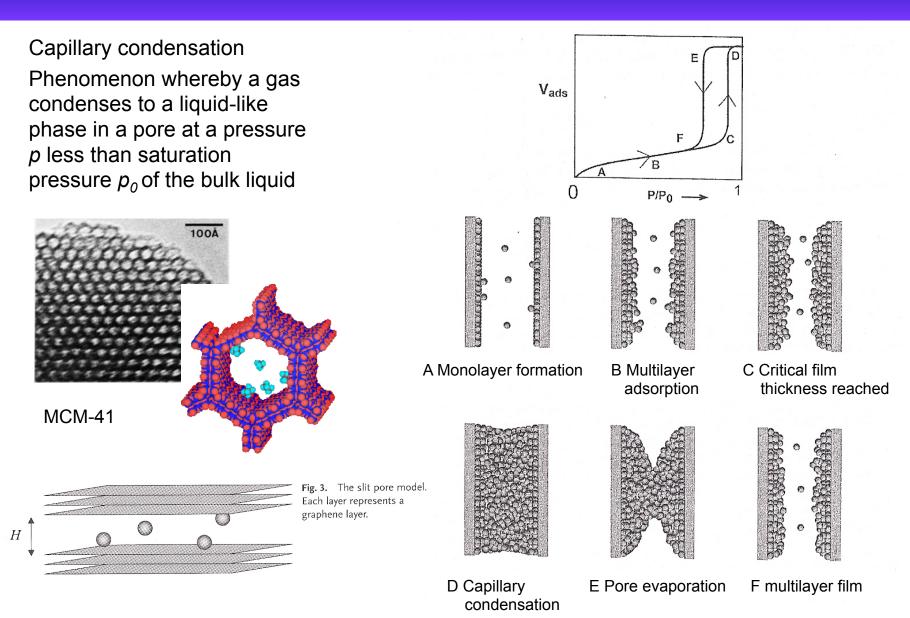
Low surface area analysis

 With nitrogen it is possible to measure absolute surface areas as low as

$$0.5-1 \text{ m}^2$$

- To measure lower surface areas the ratio between the number of molecules in the void volume and adsorbed molecules must be reduced
- Super-cooled liquid Kr (77 K) has a saturation pressure of 2.63 torr, i.e., the number of molecules in the free space of the sample cell is significantly reduced compared to nitrogen (1/300th)
- Cross sectional area of Kr varies depending on the adsorbent surface / wetting behavior in "solid" state
- But krypton has been established for low surface area measurements (0.5-0.05 m²)

Capillary condensation in mesopores (2 - 50 nm)



The wider the pore size distribution the less sharper is the pore condensation step

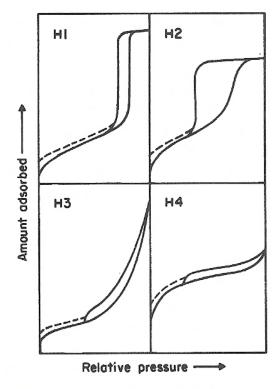


Fig. 3. Types of hysteresis loops

- H1 well defined cylyndrical pore channels
- H2 disordered pores (pore blocking, percolation phenomena)

- H3 non-rigid aggregates of plate-like particles (slit-shaped pores)
- H4 narrow slit pores including pores in the micropore region

Low pressure hysteresis

no accurate pore size analysis possible!

- Changes in the volume of the adsorbentSwelling of non-rigid pores
- •Irreversible uptake of molecules in the pores
- Chemisorption
- * K.S.W. Sing et al., Pure Appl. Chem. 57 (1985) 603.

The relative pressure where the pore condensation occurs depends on the pore radius The Kelvin equation provides a correlation between pore radius and pore condesation pressure

Assumptions

- Pores of cylindrical shape
- No fluid-wall interactions

$$\ln \frac{p}{p_0} = \frac{-2\gamma V_l}{r_p RT} \quad \begin{array}{c} V_l & \text{liquid molar volume} \\ r_p & \text{pore radius} \\ r_k & \text{critical radius} \end{array}$$

surface tension of liquid nitrogen

R universal gas constant

statistical thickness

$$r_k = \frac{4.15}{\log(p_0/p)} \text{ Å}$$

$$r_p = r_k + t$$

$$t = 3.54 \left[\frac{5}{\ln(p/p_0)} \right] \text{Å}$$

- The depth of the adsorbed multilayer film present prior to condensation is expressed in form of the statistical thickness t (number of layers times thickness of one layer)
- The thickness of one closed-packed hexagonal N₂ layer is 3.54 A
- t is a function of the relative pressure
 The empirical equation depends on the adsorbent

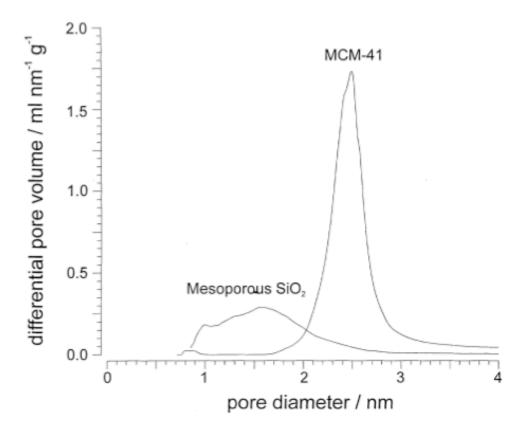


Fig. 3. Pore-size distribution according to the BJH method.

S. Storck et al. / Applied Catalysis A: General 174 (1998) 137-146.

The shape of the isotherm does not depend only on the texture of the porous material, but also on the differences of the thermodynamic states between the confined fluid and the bulk fluid

H1 - independent cylindrical pores (MCM-41, SBA-15) "Independent pore model"

- Pore condensation is associated with metastable states of the pore fluid in ordered materials
- The desorption branch of the hysteresis loop reflects the equilibrium phase transition
- Methods, which describe the equilibrium phase transition (BJH) have to be applied to the desorption branch
- Applicable also to three-dimensional network of pores

H2, H3 – disordered, connected pores

- Origin of hysteresis not yet completely understood
- Pore blocking (inkbottle pores) associated with the desorption process
- Analysis of the adsorption branch (NLDFT-spinodal condensation method, Kelvin equation based approach calibrated for the adsorption branch)

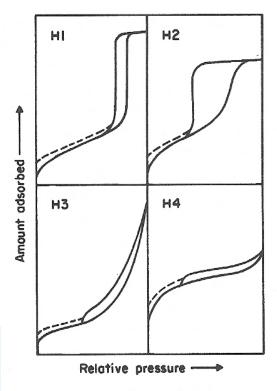
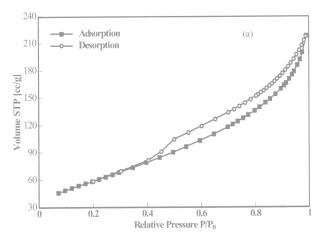


Fig. 3. Types of hysteresis loops

Tensile Strength Effect (TSE)



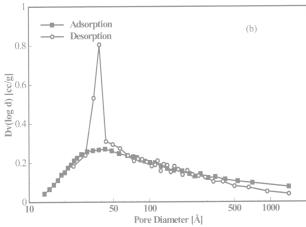


Figure 8.7 (a) Nitrogen adsorption/desorption at ~77 K on a disordered alumina catalyst; (b) BJH pore size distribution curves from adsorption and desorption branches.

Table 2
Examples of erroneous assignment of the TSE to real pores at approximately 3.8 nm

System	Peak position in PSD (nm)	Comments in original manuscript	Ref.
ZSM-5 zeolite with uniform 4 nm pores	4	Creation of uniform 4 nm pores upon alkaline treatment of ZSM-5 zeolite	[26]
Dealuminated Al-rich zeolites	3.8	Narrow peaks suggesting homogeneous pore sized system around 4 nm	[75]
V-MCM-41 and Cr-MCM-41 with hierarchical structure	2.5–2.7, 3.9	Bimodal PSD in V-MCM-41 and Cr- MCM-41 by simultaneously growing of two types of micelles	[76]
Thermally stable MCM-41 with complementary textural porosity	2.5–2.6, 3.6	Bimodal framework and textural PSDs suggesting complementary porosity	[77]
Vanadium-doped MCM-41	2–3, 3.8	V-MCM-41 with bimodal PSD, only the smaller diameter being variable	[78]
Novel aluminosilicate with bimodal mesopore distribution	2.6, 3.8	Novel aluminosilicate with bimodal PSD and possible application in catalysis and separations	[79]
Micro- and mesoporous titanosilicate catalysts	0.8, 3.6	Bimodal narrow PSD at 0.8 and 3.6 nm derived from Ar adsorption at 77 K	[80]
TiO ₂ photocatalysts by dissolution of titania-silica binary oxides	Micro ^a , 3.9	Mesoporous photocatalyst with uniform pore size of 4 nm	[81]
Novel preparation of high surface area TiO_2 catalyst	3.5 , ∼10	Variable mesopore size around 10 nm and a fixed contribution at 3.5 nm, suggesting bimodal porosity	[82]
Mesoporous zirconium oxide by sol-gel procedure	3.6	Sharp mesopore distribution and high sur- face area	[83]
Pd/Al ₂ O ₃ by sol-gel preparation	3.6, 4.5	Narrow PSD centered at 3.6 nm, finally becoming bimodal at 3.6 and 4.5 nm	[84]
Vanadium phosphorous oxide from vanadyl <i>n</i> -butylphosphate	Micro ^a , 4.4	Bimodal distribution with narrow mesopore size at 4.4 nm derived from Dollimore-Heal pore size model	[85]
Preparation of porous SiO2 from kaolinite	3.8	Unimodal pores with average size of 3.8 nm	[86]

^a The micropore size is not further specified in the manuscript.

Pore network effects

J.C. Groen et al. / Microporous and Mesoporous Materials 60 (2003) 1–17

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